

If you pour a cup of coffee, it cools more rapidly at first, then less rapidly, finally approaching room temperature. You can show the relationship between coffee temperature and time *graphically*. Figure 1-1a shows the temperature, y , as a function of time, x . At $x = 0$, the coffee has just been poured. The graph shows that as time goes on, the temperature levels off, until it is so close to room temperature, 20°C , that you can't tell the difference.

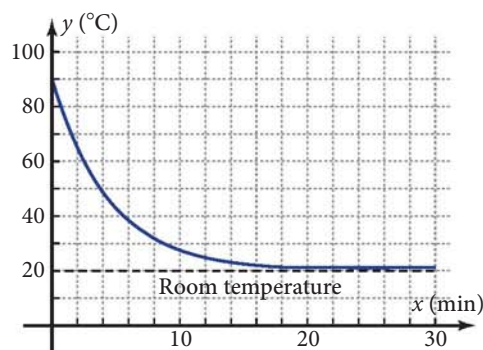


Figure 1-1a



This graph might have come from numerical data, found by experiment. It actually came from an **algebraic** equation, $y = 20 + 70(0.8)^x$.

x (min)	y ($^{\circ}\text{C}$)
0	90.0
5	42.9
10	27.5
15	22.5
20	20.8

From the equation, you can find **numerical** information. If you enter the equation into your grapher and then use the table feature, you can find these temperatures, rounded to 0.1°C .

Functions that are used to make predictions and interpretations about something in the real world are called **mathematical models**. Temperature is the **dependent variable** because the temperature of the coffee depends on the time it has been cooling. Time is the **independent variable**. You cannot change time simply by changing coffee temperature! Always plot the independent variable on the horizontal axis and the dependent variable on the vertical axis.

The set of values the independent variable of a function can have is called the **domain**. In the coffee cup example, the domain is the set of nonnegative numbers, or $x \geq 0$. The set of values of the dependent variable corresponding to the domain is called the **range** of the function. If you don't drink the coffee (which would end the domain), the range is the set of temperatures between 20°C and 90°C , including 90°C but not 20°C , or $20 < y \leq 90$. The horizontal

line at 20°C is called an **asymptote**. The word comes from the Greek *asymptotos*, meaning "not due to coincide." The graph gets arbitrarily close to the asymptote but never touches it. Figure 1-1b shows the domain, range, and asymptote.

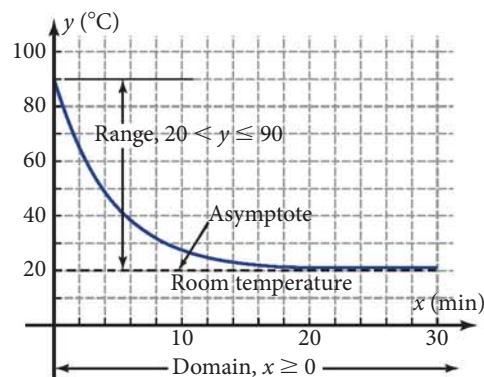


Figure 1-1b